

## Lecture 3 Chapter 7: Interest Rates and Bond Valuation

- Why study bonds ?
  - clean application of the Time Value of Money
  - central to corporate finance
  - central to monetary policy
  - central to financial speculation
- But first ... Unfinished Business!
  - Section 6.4: Loan Types and Amortization

## Loan types and Loan Amortization

- **Pure discount loan**
  - *Borrower receives money today and repays a single lump sum at some time in the future.*
  - Example:  
*The XYZ firm wishes to finance its investment project by issuing a pure discount bond. They expect to be able to repay a sum of \$35,000 in 7 years. How much will they receive today if investors want a return of 12% ?*

## Loan types and Loan Amortization

- **Amortized loan**

- Borrower receives money today and repays both interest and portions of the principal in each period.
- Example:
 

*You want to put \$3000 into your RRSP before the February 28<sup>th</sup> deadline, but you don't have the cash. Your bank offers to lend you the \$3000 at a monthly interest rate of 0.5%, provided you pay it back in 12 monthly payments. You need to find the size of the payments to see whether you can afford it.*
- One way of looking at the amortization of a loan is to say that the payments give a PV equal to the amount borrowed.
  - Taking out an amortized loan is like selling an annuity to the bank

## Loan types and Loan Amortization

Month	Outstanding Balance	Interest due	Payment	Reduction of o/s bal.	New balance
1	\$3,000.00	\$15.00	\$258.20	\$243.20	\$2,756.80
2	\$2,756.80	\$13.78	\$258.20	\$244.42	\$2,512.38
3	\$2,512.38	\$12.56	\$258.20	\$245.64	\$2,266.75
4	\$2,266.75	\$11.33	\$258.20	\$246.87	\$2,019.88
5	\$2,019.88	\$10.10	\$258.20	\$248.10	\$1,771.78
6	\$1,771.78	\$8.86	\$258.20	\$249.34	\$1,522.44
7	\$1,522.44	\$7.61	\$258.20	\$250.59	\$1,271.85
8	\$1,271.85	\$6.36	\$258.20	\$251.84	\$1,020.01
9	\$1,020.01	\$5.10	\$258.20	\$253.10	\$766.91
10	\$766.91	\$3.83	\$258.20	\$254.37	\$512.54
11	\$512.54	\$2.56	\$258.20	\$255.64	\$256.91
12	\$256.91	\$1.28	\$258.20	\$256.92	\$-0.01

# Loan types and Loan Amortization

- **Interest-only loans**

- *Borrower receives loan today and pay interest each period and repays the entire principal at some point in the future.*

- Example

- XYZ decides to finance its project by issuing an interest only loan that will pay investors \$35,000 in 7 years and interest payments of 12% compounded annually over a period of 7 years.*

- How much can the company expect to receive from this financing?
- How does the answer compare to the pure discount loan ?

Any ideas why ?

## Bonds (chapter 7)

- **Definition:** Long-term debt of a corporation or government
- Usually in the form of an interest-only loan
- Important components:
  - **Face value:** Amount to be repaid at maturity
  - **Coupon:** Regular (interest) payments made to the bond holder; expressed in the **coupon-rate** as a percentage of the face value
  - **Maturity:** The date when the face value is repaid and the coupon payments end

## Bond Basics

- The coupon, the face value and the maturity date are all determined by the bond issuer; these are written into the bond.
- The amount borrowed is determined by the bond's price in the primary market; this is market-determined.
- Standard corporate bonds have a face value of \$1000.
- Coupons are typically paid semi-annually.
- Coupon rate is an APR:
  - 10% rate means \$50 every 6 months (i.e. 1/2 of 10% of \$1000)
- Question: Is the coupon rate a simple interest rate or a compound interest rate?

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## Bond Valuation

*A corporate treasurer has to finance \$2 million of new spending by issuing bonds with a coupon rate of 6.5% and a maturity of 4 years. If the bonds have a face value of \$1000 each, how many bonds must be issued?*

No, not 2,000 bonds. It depends on the (primary) market price of the bonds. What would you be willing to pay for a bond? => PV

To calculate the PV, we look at its cash flows:

- **coupon payments:** look just like an annuity!
- **face value:** looks just like a future value!

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## Bond Valuation (cont.)

- So what is the bond's market price?
- The PV of the bond must be PV of its cash flows
- The PV of its cash flows must be the sum of the PV of the different parts of its cash flows
- In general Bond Value = PV(coupon payments) + PV(face value) =

$$\frac{C}{r} * \left[ 1 - \frac{1}{(1+r)^t} \right] + \frac{F}{(1+r)^t}$$

- where
  - $C$  is the coupon payment per period =  $F * \text{coupon rate per period}$
  - $r$  is the periodic interest rate
  - $t$  is the number of periods until maturity
  - $F$  is the face value

## Bond Valuation (cont.)

- If we assume yearly coupon payments, and a market interest rate of 9%, what would be the price of the bonds issued by the company?
- How many bonds would the treasurer need to issue to raise the \$2million?

# Yields

- **3 Bond-related rates to keep straight:**
  - **Coupon rate:** annual coupon payments as a fraction of face value ? fixed by the company at  $C/F$
  - **Current yield:** annual coupon payments as a fraction of market price:  $C/P$
  - **Yield to maturity:** discount rate that makes the bond's PV equal its market price (also called **internal rate of return**) ? set by the market at  $r$
- **Let's look again at the 4-year bond example.**
  - Coupon rate = 6.5% or  $\$65 / \$1000$
  - Current yield = 7.07% or  $\$65 / \$919.01$
  - Yield to Maturity = 9%

## Semi-Annual Valuation

- We assumed that coupons were paid annually, but semi-annual is the norm.
- **How much difference does it make to bond prices?**
- Let's use the same formula, but with semi-annual coupon, interest rate and number of periods.
  - $C =$
  - $n =$
  - $r =$
  - *Bond value* =

# Yields

- Corporations generally try to set the coupon rate equal to the yield-to-maturity at the time of issue.
- If they do this, then what is the price of the bond?
  
- When coupon rate > yield-to-maturity, the price of the bond is \_\_\_\_\_ the face value.
- When coupon rate < yield-to-maturity, the price of the bond is \_\_\_\_\_ the face value.

Example:

*A 4-year bond with a 14% annual coupon sells for \$1200. What is the yield to maturity?*

The equation to solve is

$$\text{Bond value} = 140 * \frac{1 - 1/(1+r)^4}{r} + 1000 * \frac{1}{(1+r)^4} = 1200$$

Solving for  $r$  is tough. Two approaches:

1. Iterate until you're "close enough"
2. let your financial calculator or computer do it

## Solving for $r$

- How to solve for  $r$  in a PV equation:
  - Guess. Try  $r = 0.1$  or some other value.
  - Calculate the PV for that value of  $r$ .
  - Is the PV too high? Then your  $r$  needs to be higher.
  - Is the PV too low? Then your  $r$  needs to be lower.
  - Return to step 1 with a better-informed guess.
- As you repeat this, you “bracket” the correct value and gradually approach the answer.
- This is not just true for bonds. In general:
  - solving PV equations for  $r$  is hard
  - this iterative approach takes you to the right answer
  - this approach is used by most calculators and computers

## Interest rate risk

- The value of a bond depends on the interest rate .
  - higher  $r$  means the PV of payments in the future will be less (higher opportunity cost) ? Lower bond prices
- Suppose you bought our treasurer’s bonds when the interest rate was 9%, but then they fell to 6.5%. How are you affected?
  - Your cash flow does not change.
  - The PV of this cash flow is now higher
  - Therefore, the market price of this bond is now higher.
- Congratulations! You just made a capital gain! How much?
- We know that at 9%, the bond price was \$919.01 and at 6.5% it is \$1000 (why?).

You made \$80.99, or 8.8% profit overnight!

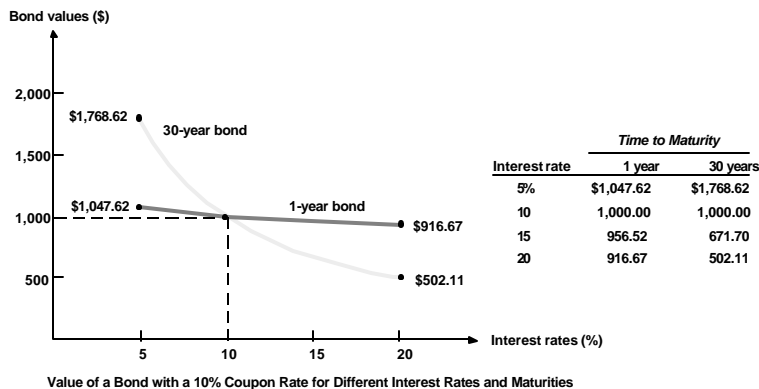
## Interest Rate Risk (cont.)

- Suppose instead of a 4-year bond, you had a 1-year bond.
  - Its price at 9% interest would be  $1065 / 1.09 = 977.06$
  - Its price at 6.5% would be \$1000.
  - capital gain =  $\$22.94 / \$977.06 = 2.35\%$
- Suppose we had a perpetuity?
  - price goes from  $\$65 / 0.09 = 722.22$  to  $\$65 / 0.065 = \$1000$
  - capital gain =  $277.78 / 722.22 = 38.5\%$
- **The longer the maturity, the more sensitive the price is to interest rate changes**

➤ Interest rate risk increases with maturity

## Interest Rate Risk and Time to Maturity

- Figure 7.2 ( page 198)



## Rate of Return on Bonds

- Rate of Return: *Earnings per period per dollar invested.*
- Returns on bonds have two components:
  - coupon payments
  - capital gains & losses due to changes in interest rates

### Never confuse YTM with RoR!

- YTM is the special case of RoR where you hold the bond until maturity.
- RoR applies regardless of whether you hold until maturity or for a shorter period.

**Example:** *Suppose you buy a 4-year bond with a 6.5% coupon when interest rates are 9%. Interest rates remain at 9% over the next year and you sell the bond after one year.*

- What is the price of the bond when you sell it?
- What RoR have you earned on your investment?

*Why does the bond's price change if the interest rate doesn't?*

- repayment of face value is closer
- coupon rate < interest rate, so coupons do not fully compensate for having to wait for repayment.  
Therefore, we have to get a capital gain in order to get our "fair" 9% RoR.

**Lesson 1** Constant interest rates need not imply constant bond prices

**Lesson 2** If interest rates are unchanged,  $r = RoR$

## Bond features

**Indenture:** written agreement between the borrower and the creditor

- Terms of the bond
  - *Registered: corporation keeps track of owners*
  - *Bearer: certificate is the only evidence of ownership*
- Security
  - *Collateral, mortgage, unsecured*
- Seniority: in case of trouble, who gets paid first?
  - *junior vs senior*
- Repayment
  - *sinking fund managed by a trustee*
- Call provisions
- Protective covenants
  - *negative vs positive*

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## Bond Features (cont)

- Debt versus Equity
  - **Ownership:** Debt holders have no control over the management of the firm, except through bond covenants
  - **Bankruptcy:** Debt holders must be paid all they are owed before equity holders get anything
  - **Taxation:** Interest payments are tax-deductible to the corporation, but taxable to the investor; dividend payments are the reverse.
- The *art* of finance: creative bonds
  - Stripped, floating, retractable, convertible, income
- Question: Is a perpetual income bond really debt or equity, and why does it matter?

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## Another risk: Bond Defaults

- **Default:** When the issuer of the bond stops making the agreed payments.
- Bondholders can sue to obtain payments or the assets of the firm unless:
  - Firm has bankruptcy protection
  - The lender is a sovereign nation
- National government bonds payable in domestic currency are typically considered “risk-free”
  - government can always print money to pay off these bonds.
- For a firm that has a chance of defaulting in the future, we can no longer count on receiving all the promised payments.
- Instead, we demand an extra yield to compensate for the possibility of default. This extra yield versus an equal-maturity government bond is sometimes called the **default premium**

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## Bond Rating

- There are companies that specialize in judging the probability of bond defaults. They publish **bond ratings**.
- The Canadian bond raters are the *Canada Bond Rating Service* (CBRS) and the *Dominion Bond Rating Service* (DBRS)
- In the US, the business is dominated by *Moody's* and *Standard and Poor's*.
  - Since capital markets are international, the US bond raters often rate non-US borrowers.
- Rating systems vary by company, class of issuer, type of instrument, etc.
- Generally, they are like school grades; A is better than B, + is better than -
  - the better the rating, the lower the probability of default
  - in bond rating, anything lower than a B is usually a failing grade
- Bonds with low ratings are politely called *non-investment grade*, and are less politely called **junk bonds**.

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## Bond Markets

- Over the counter markets
  - Trade takes place on a dealer-to-dealer basis; no central exchange to coordinate
  - Huge volume and huge variety of bonds
  - Lack of transparency
  - Consequently, it is often difficult to find a market price
- To price a bond that has no recent transactions:
  - Find a bond of similar maturity and risk (bond rating)
  - Use the yield-to-maturity of that bond to discount the cash flows of the bond that you want to price and obtain a present value

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## The Yield Curve

- YTM varies with maturity. This is called the **term structure of interest rates**
- A graph of YTM versus maturity is called the **yield curve**.
- Typically, short-term yields < long-term yields
  - if not, we say the yield curve is “inverted”
  - inverted yield curves have been linked to oncoming recessions, but that’s another story
- If long-term YTM’s are higher, why would anyone buy short-term bonds?
  - **Risk:** We saw rates of return on long-term bonds are more sensitive to changes in interest rates than those of short-term bonds. If you dislike risk, you’ll demand a reward for facing risk.
  - **Expectations:** You might be expecting short-term interest rates to rise.

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## Inflation and Interest Rates

- **Nominal rates:** *Interest rates or rates of return that have not been adjusted for inflation*
- **Real Rates:** *Interest rates or rates of return that have adjusted for inflation*
  - We are concerned not with the number of dollars we will have, but with how much those dollars will buy

The Fisher effect:

$$1 + r_{nominal} = (1 + r_{real}) * (1 + inflation\ rate)$$

$$\Rightarrow r_{nominal} = r_{real} + inflation\ rate + r_{real} * inflation\ rate$$

$$\sim r_{real} + inflation\ rate$$

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## Inflation (cont)

- The important thing to remember is to **match** *real cash flows* with *real rates* and *nominal cash flows* with *nominal ones*.

- Example:

*You want to plan for 20 years of retirement.*

*You think you can live on \$24,000/yr. (in current purchasing power).*

*You think the Bank of Canada will keep inflation at 2%.*

*Long-term interest rates are 5.5%.*

*a) How much do you need upon retirement to finance this?  
(i.e. to buy a 20-year annuity for this amount?)*

*b) You want to retire 40 years from now. How much do you have to save every year to have enough saved when you retire?*

- For a real world example check out :  
[http://www.tdcanadatrust.com/planning/rrsp\\_planning\\_calc.jsp](http://www.tdcanadatrust.com/planning/rrsp_planning_calc.jsp)

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## What we know now

- Loan types
  - Discount
  - Amortized
  - Interest-only
- Bond characteristics
  - Face value / coupon / maturity
- How to value bonds
  - Discounted cashflow
  - Difference between coupon rate, current yield and yield to maturity
- Bond features
  - Terms / security / seniority / protective covenants
  - Debt versus equity / financial engineering
  - Bond markets: over-the-counter
- Bond Risk
  - Interest rate risk
    - Term structure of interest rates / the yield curve
    - Inflation
  - Default Risk
    - Credit ratings

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## A few translations

See also: <http://www.granddictionnaire.com/>

Maturity	<i>l'échéance</i>
Face value	<i>la valeur nominale</i>
Coupon	<i>le coupon</i>
Coupon rate	<i>le taux de coupon</i>
Yield	<i>le rendement</i>
Coupon yield	<i>le rendement coupon</i>
Current yield	<i>le taux actuariel</i>
Dividend yield	<i>le rendement des actions</i>
Effective yield	<i>le rendement effectif ou réel</i>
Yield to maturity	<i>le taux actuariel ou le rendement actualisé</i>
To yield (financial)	<i>rapporter</i>

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